STRESS ANALYSIS OF TRANSVERSE SHIP FRAMES LOWELL P. DANIELS WARD J. DAVIES ALCOUPTE, THUT La





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Je r cir:

In accordance with the requirements for the Deree of Naval Engineer, we submit herewith a thesis entitled, "Stress Analysis of Transverse Ship Frames."

Respectfully,



ACIAIL A DG MINT

The suthers wish to express their sincere appreciation and indebtedness to Professor Larries H. Morrie for his at jestion of the thesis topic and his patient juillance during the investigation.

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SUMMARY

blect:

The purpose of this investigation was to compare the results of two theoretical methods of calculating stress in a ship's transverse frame with an experimental model analysis.

Frocedure:

The experimental stress analysis for a ship's frame was made using a planar celluloid model and the Beggs method. Calculations were made using the clastic center method based on the law of virtual work and the method of Frof. W. Hovgaard to determine influence lines of stress due to vertical and morisontal unit loads. The results were compared using the experimental results as a basis of comparison.

Results:

The families of six influence lines obtained by each of the three methods of analysis agreed very closely.

Conclusions:

The experimental results verified that the methods of calculation of stress using twelve integration stations gave consistent accuracy. The clastic center method required less



computation work and attained a slightly greater degree of accuracy.

Recommendations:

It is recommended that further work be undertaken

(1) to determine the amount of error resulting from the simplifying assumptions used and (2) to obtain a similar comparison for a ship with two or more decks. The simplifying assumptions were that the moment of inertia varied as a continuous function and that the effects of axial force and shear were negligible. Further model analysis should be made using models that have a greater degree of stiffness to better overcome frictional forces.



I. PRODUCTI A

The determination of stress in the transverse frame of a smill presents a difficult problem because of the complicated structure involved. A number of methods of solution have been devised. Dr. J. Bruhn in reference (2) proposed a nothed based on Jastigliano's principle of heast work.

Frof. J. A. Hovgaard have a method based on deflections in reference (5). In addition to these methods advanced by naval architects, other methods applicable to any structure in the form of a closed ring are available. One of these is the application of the law of virtual work frequently used by civil engineers for indeterminate structures.

The above methods are all based on mathematical hypothesis and are completely accurate only if the mathematical expressions used exactly represent the actual structure.

This is impractical for the ship frame, and simplifying assumptions are necessary in order to make the computation possible in a reasonable amount of time. The work of interration in the theoretical methods is reduced by using as few stations as possible consistent with reasonable accuracy.

The actual moment of inertia varies abruptly and frequently, but it is generally assumed to be represented by a continuous curve faired through the several values. This curve will not necessarily correspond to the actual changes in the moment



of inertia and thus a discrepancy from the actual moment of inertia (a) exist at the point represented. A second assumption usually made is that the effects of axial and sheer distortion are small relative to that of the bending distortion and are neglected.

This investigation determines the influence lines for each of the redundant forces due to unit vertical and horizontal loads. These influence lines are determined experimentally and theoretically by two methods. The two theoretical methods are compared to the experimental results and evaluated for accuracy and ease of computation.

The apparatus used to determine the influence lines experimentally consisted of a planar celluloid model which had a moment of inertia proportional to the actual ship frame. The frame was cut at the keel and a Beggs deformeter gage installed which produced distortions of a known magnitude. The deflections produced by these distortions at selected points were then measured with a micrometer microscope. The ordinates of the influence line for a load applied at these points are then determined by application of the Muller-Breslau principle.

One of the theoretical methods of determining the influence lines consists of utilizing the law of virtual work with the redundants located at the elastic center. The other is the method of Prof. Hovgaard as described in reference (5).



PROCEDURE

The procedure used in this investigation for determining the influence lines consisted of four parts (1) setting the conditions of the problem and determining the data necessary for the experimental and theoretical methods of analysis (2) manufacture of the model and performance of experimental work (3) calculation by the method of virtual work using the elastic center and (4) calculation by the Novaerd method.

A transverse frame of a modern destroyer, which is typical of haval construction, was selected as the source of all data. The mount of inertia and distance of the neutral axis from the molded line were determined at twenty-five points. This relatively large number of points was used in order to make the values of moment of inertia approximate the actual frame as closely as possible. Large-scale curves were plotted of moment of inertia versus distance along the molded girth and of neutral axis distance from molded line versus distance along the molded girth. The coordinates of points on the neutral axis were determined graphically from a drawing of the molded line. Appendix A describes in more detail how the fundamental data were obtained.

A planer model, having the shape of the neutral axis and moment of inertia proportional to that of the prototype, was made. It was cut from a sheet of celluloid and filed

until the depth gave the required moment of inertia. The method of calculating the model dimensions and the actual micrometer measurements obtained may be found in Appendix B. Next the frame was cut at the location of the keel and the ends clamped into the two halves of a Beggs deformater gape. The right half of the gage was screwed to the table.

Briefly, the experimental work consisted of introducing known distorthous unto the model structure and measuring the deflection of each point at which an influence line ordinate was desired. Distortions of a known magnitude are introduced by inserting the various sizes of calibrated plugs into the Beggs deformeter gage. The horizontal deflection of a point measured by the microscope gives the data for determining the ordinate to the influence line of a redundant due to a unit horizontal load. Similarly the vertical deflection ives the data for the influence line of a redundant due to a unit load applied vertically. The ordinate of the influence line for a redundant is equal to minus one times the ratio of the measured deflection to the introduced deflection. The deflection for each of 24 points around the frame was measured to determine each influence line. Due to symmetry of the structure only the 12 readings for one side of the model are necessary; however, the other readings may be used as a check. The details of the experimental work are explained more fully in Appendix B.



Inted by the method of virtual work with the location of the redundants at the elastic center. The location of the redundants at this point eliminates the solution of simultaneous equations. For comparison with the redundants determined experimentally the redundants at the elastic center were transferred to the same location. The details of the calculation by the elastic center method are given in Appendix C.

The other method of calculation utilized the method of the late Prof. W. Hovgaard to determine the influence lines for each redundant. This method requires the solution of simultaneous equations. The calculation details are given in Appendix D.



RASULTS

The results of this investigation consist of the influence line ordinates for moment, thrust and shear caused by unit vertical and horizontal loads. The results are tabulated and compared in Tables I and II.

Small-scale plots of the results are shown in Figures I, II, and III. The curves represent the values found by all three methods. To plot the results of all methods would require too large a scale to be practical. The results are best compared in tabular form.

Figure VI is an aid in visualizing the significance of the results.



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Comparison

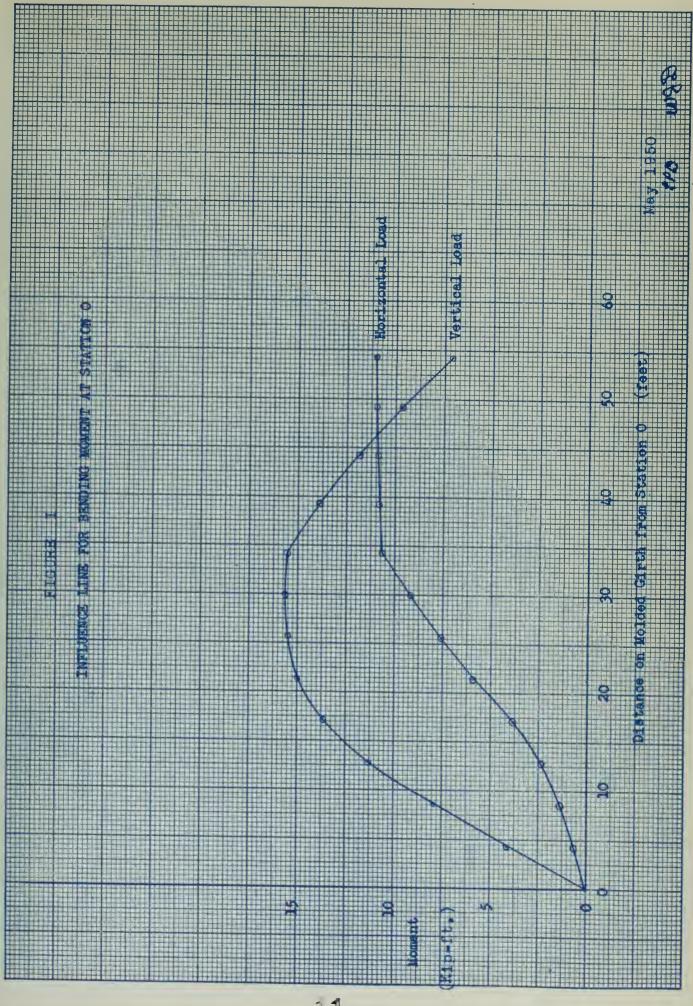
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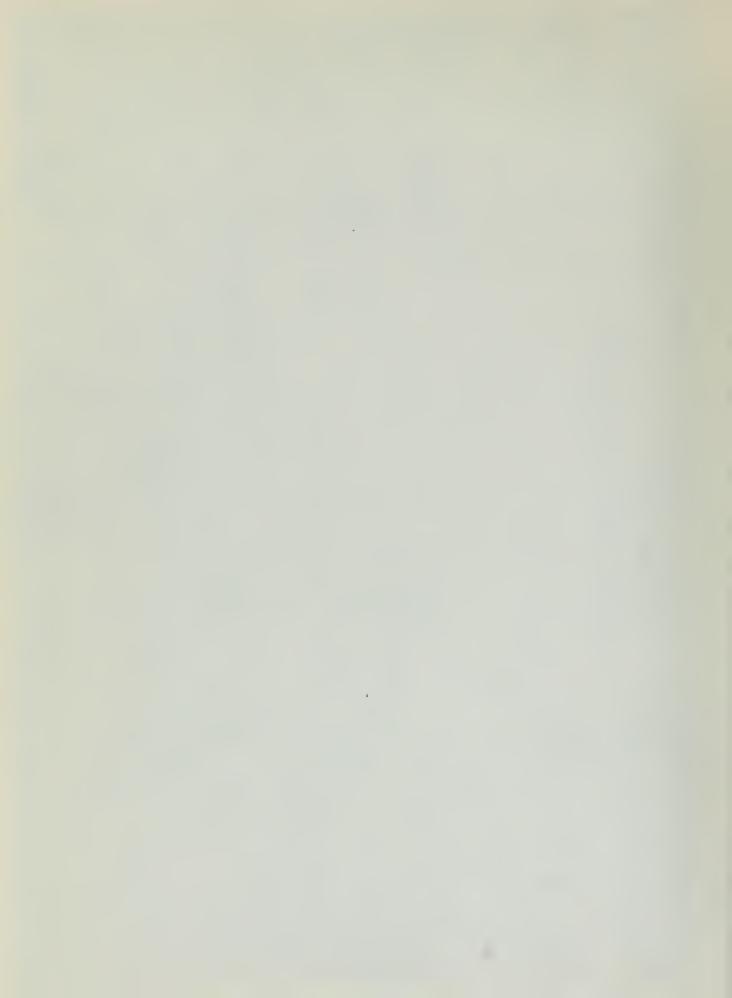


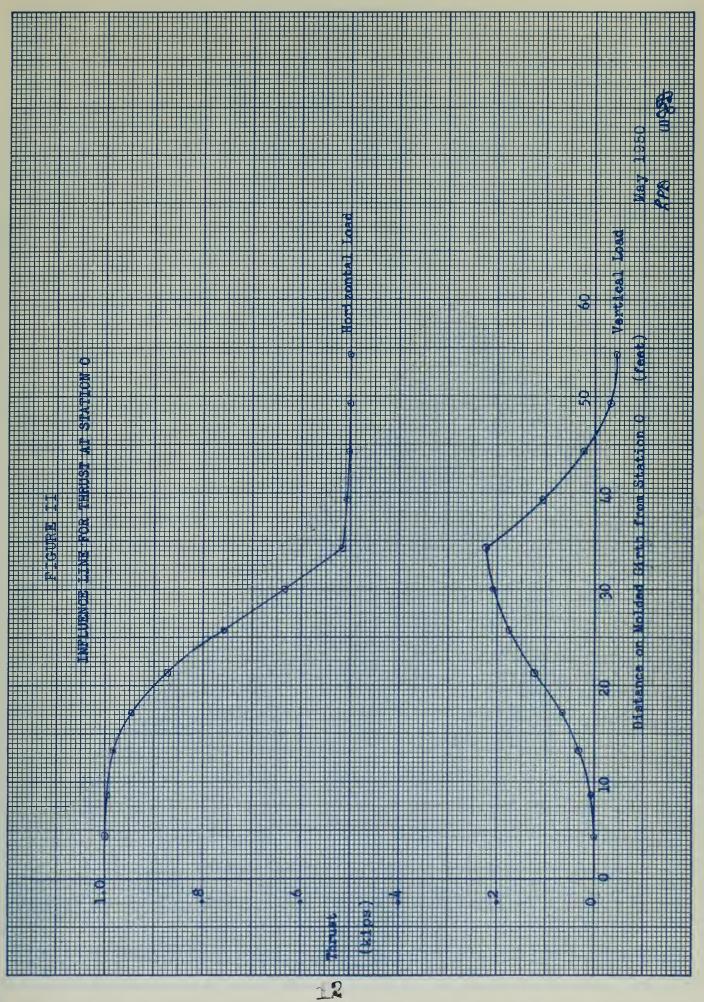
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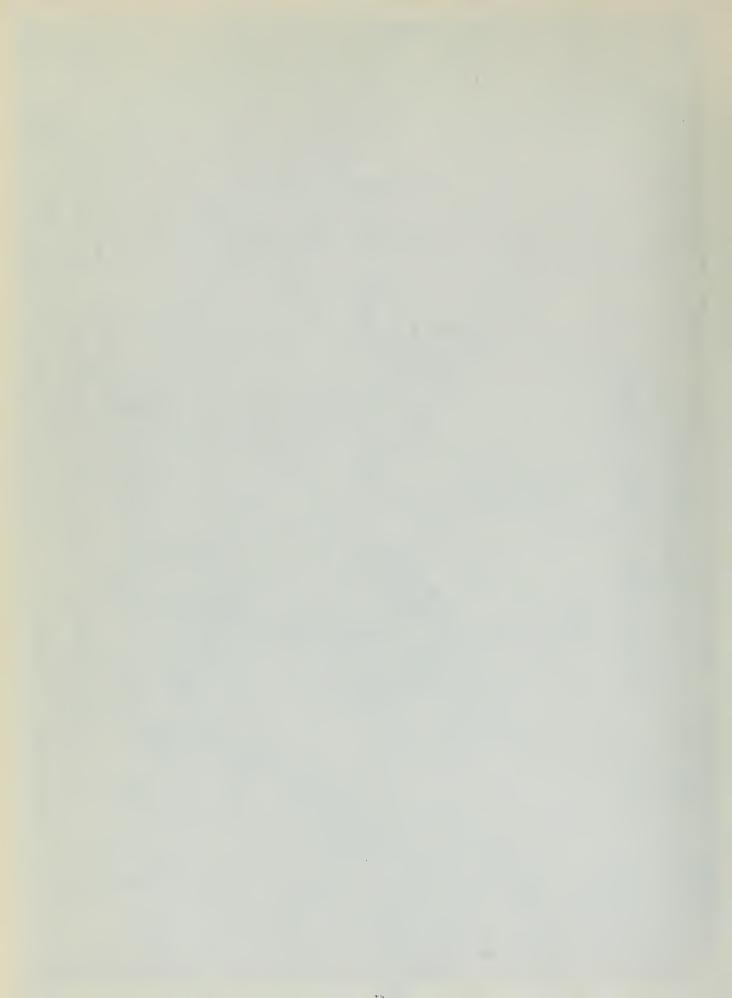
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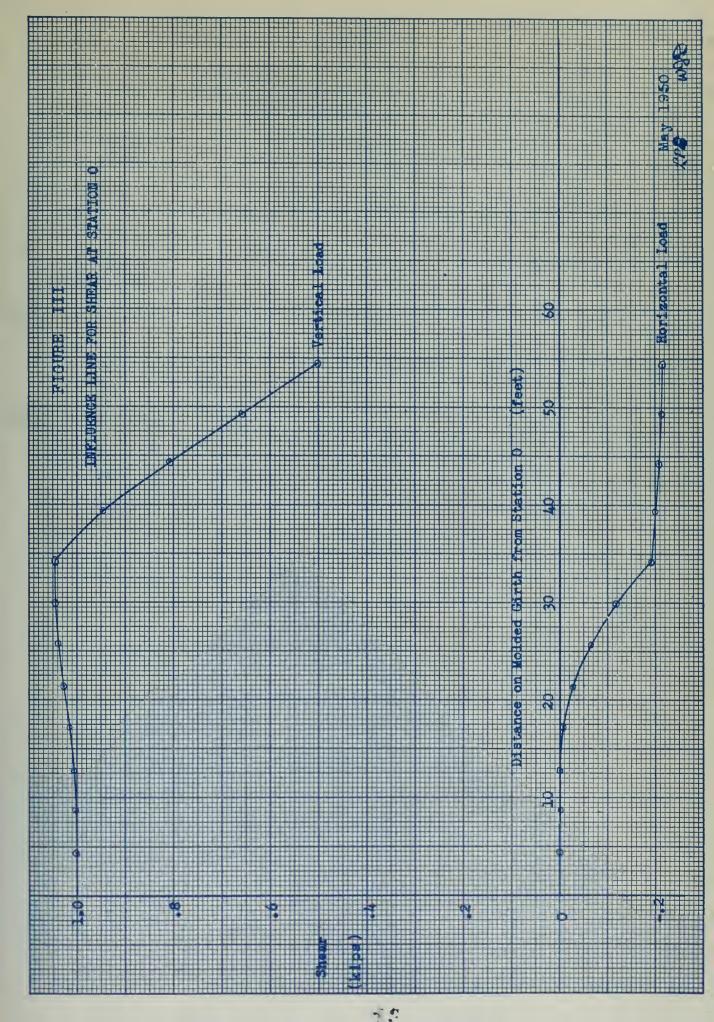














DISCUSSIVE OF RESULTS

The three methods of obtaining the influence lines liven in Tables I and II show very good agreement. For purposes of comparison the influence line determined experimentally was selected as a base.

Experimental techniques are always subject to measurement errors and to physical phenomena beyond the control of the experimenters. Every effort was made to minimise these types of errors. The principal errors applicable to this investigations are listed below:

- (1) Friction forces in the model mounting apparatus of sufficient magnitude to prevent normal deflection.
- (2) Alignment errors in mounting the model in the Beggs apparatus and in orienting the microscope.
- (3) Uncertainty of microscope readings because of personal observation errors.
- (4) Arror in the calibration coastant obtained for the microscope.
- (5) Errors in the introduced distortions caused by the Beggs plues not being the stated size by .±0.0001".
- (6) Errors in the model manufacture where the filed depth differed from the theoretical. These destroyed strict proportionality between the model and prototype moment of inertia.



- (7) Variations in the modulus of elasticity due to non-homogeneity of the model material.
- (3) Distortions of the model due to localized thermal expansions.

The authors estimate the cumulative effect of the above errors to be 12 microscope units. The probable error incurred will only be 5 microscope units. This error will affect the threat and shear redundants by the amount of ±.0183 and the moment redundant by ±.179. Thus in Tables I and II any differences between the experimental and the calculated results which are of smaller magnitude lie within the probable experimental error. It is noted that nearly all the high percentage errors occur where the magnitude of the readings is very small and could be due entirely to this cause. Considering the differences of results which are outside the magnitude of the experimental error the maximum percentage difference was 2.88%.

The two methods of calculating the influence lines should have given identical results since they are both based on correct mathematical theories and the same basic data were used for each method. The disagreement between the results of the two methods can be attributed to: (1) solution of simultaneous equations in the Hoveaard method, (2) transfer of redundants from one location to another, and (3) errors in computation. The equations obtained by the Hoveaard method



are those of straight lines with a very small angle of intersection. This poorly defined intersection makes it possible to obtain several different values depending on the procedure used in climinating variables during the solution of the simultaneous equations. The procedure followed in this investigation minimized this error although it could still be detected. Transfer of redundants caused magnification of any small errors that existed to a size where they could become significant. This additional step was taken for the sole purpose of making the redundants alike and would normally not be necessary. Arithmetical errors in computations of this magnitude are difficult to climinate completely but the authors have made exhaustive checks and feel assured that none exist.

The remainder of the discrepancy between the theoretical and experimental solutions may be attributed to the more accurate integration of effects by the model and the neglect of axial stress and shear effects in the computations. The model was constructed with the moment of inertia proportional to the prototype at 41 points while only 12 points were used in the computations. This difference would tend to make the model results more accurate. Axial stress and shear stress effects are entirely neglected in the computations while in the model they are partially taken into account. The effect cannot be considered comparable to that in the prototype because the cross sectional shapes are not similar.



The work of computation by the elastic center method was found to be clightly less than for the Hovgaard method. The shound of computation was nearly equal for both in the initial and intermediate parts of the work. However the last part of the Hovgaard method consists of the solution of simultaneous equations which take appreciably longer than the divisions in the last part of the elastic center method.

The solution of stress in a transverse ship's frame may be obtained by the use of influence lines as in this investigation if desired. Solution by means of influence lines is approximately five times more work of computation than a direct singular solution for a specific loading system. However the influence lines can be determined by a mechanical procedure once a form is set up for any given type of frame, and plotting the ordinates provides a ready means of detecting errors in the computation. Influence lines can be used for any system of loading without change and therefore are flexible for determining changes in loading systems. The choice of influence lines over a singular solution will depend on the value attached to the above factors in any particular case.



CONCLUSIONS

- 1. Experimental analysis verifies that calculation of the indeterminate redundants by either the elastic center or Hovgaard methods is accurate to about 3 per cent for this type of frame if only 12 integration stations are used.
- 2. The clastic center method requires somewhat less time for calculation than the Hovgaard method because of the elimination of simultaneous equations.
- 3. In the Hovgaard method the simultaneous equations that must be solved are quite sensitive to small errors which may reduce the accuracy.
- 4. The Beggs method of experimental analysis can be relied on for good results and requires only models that are inexpensive and easy to make.
- 5. Plotting influence lines grovides a check on the accuracy of the results.
- 6. Influence lines provide a more satisfactory solution than a singular solution for a specific leading system under certain circumstances.



RECULTING TIME

- 1. It is recommended that an investiation be made to deternine the amount of error resulting from the simplifying assumptions that the moment of inertia varies as a continuous function and that the effects of axial stress and shear stress are negligible.
- 2. This investigation should be extended to the case of a ship having two or more decks. It is expected that the elastic center method for computing stress will prove to have a more marked superiority over the Hovgaard method than was shown in this investigation.
- 3. To increase the accuracy, by reducing the frictional offects, a stiffer model should be used. The frame could be stiffened by increasing the thickness of the material, by increasing the depth of the frame, or reducing the scale of the linear dimensions.



APPENDIX



APPENDIX A

Description of Assumptions and Formulation of the Characteristics of the Frame

As a basis for analysis a transverse whip frame representative of naval construction was desired. Transverse frame 141 1/7 of the DD692 class destroyor, Budhips Plan No. 565652, was arbitrarily selected for study. In the analysis of this frame the following assumptions are made:

- (1) The moment of inertia of the frame is not affected by the longitudinals, lightening holes, or cable runs that pierce the web.
- (2) One frame space of shell plating is considered to be effective. This is in accordance with the U.S. Navy practice as given in Bureau of Ships Memorandum No. 447.
- (3) The shell plating is assumed to lie on the molded line as it would with welded construction. With the actual type of in and out plating used in this frame the neutral axis was found to vary by as much as 0.603°. In order to avoid a discontinuity in the neutral axis some correction was necessary. It was done by this assumption so as to avoid considering a greater moment of inertia than exists at any point. The error is on the conservative side.
- (4) The frame was considered to be symmetrical on the



port and starboard sides.

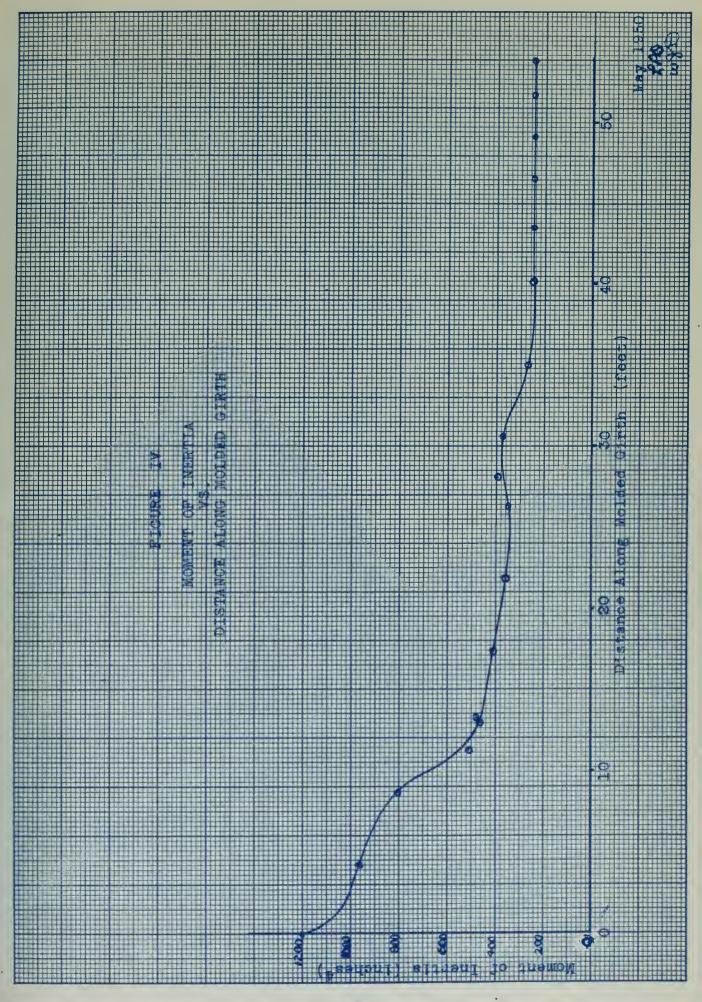
The moment of inertia and the distance of the neutral axis from the molded line for this frame were calculated at 25 points along one half the girth. This relatively large number of points was used so the data would more closely approximate the conditions of the actual frame. The results of this calculation are shown in Table III. From these results large-scale plots were made of moment of inertia vs. distance along one half the girth of the molded line and the neutral axis distance from the molded line vs. distance along one half the girth of the molded line. Small-scale copies of these curves are shown in Figures IV and V respectively.

The offsets representing the shape of the neutral axis were obtained in the following manner. A large-scale drawing of the molded line was made. On this was constructed the neutral axis from distances read from Figure V. Twelve stations were selected for use in the calculations to give the usual degree of accuracy. It was desirable that one station be located at the deck edge because of a possible discontinuity. To do this the deck was divided into four equally spaced stations of 5.031 ft. The side shell was divided into eight equally spaced stations of 4.285 ft. These 12 points were located on the neutral axis and the offsets obtained. These are given in Table IV.

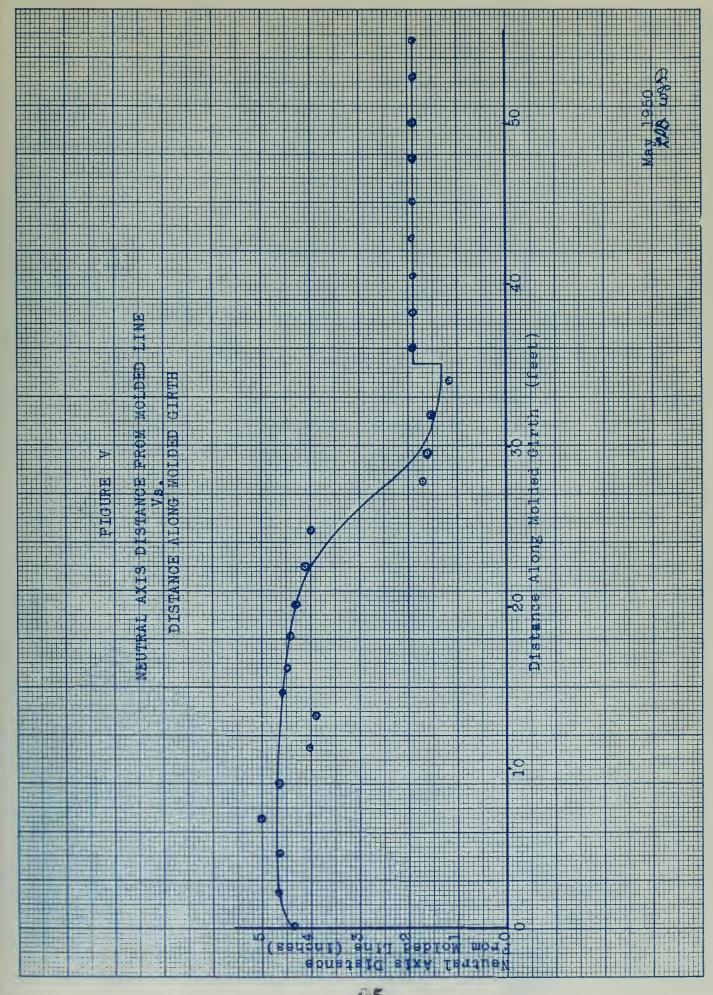


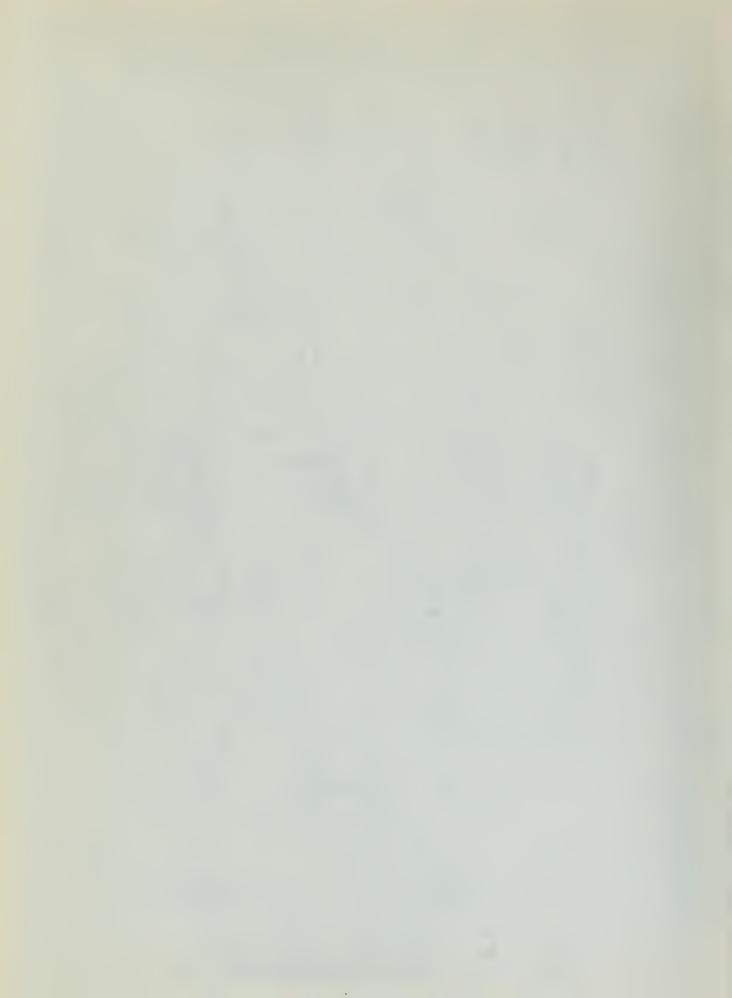
Table III
Homent of Inertia and Neutral Axis
Distance from Molded Line on Prototype

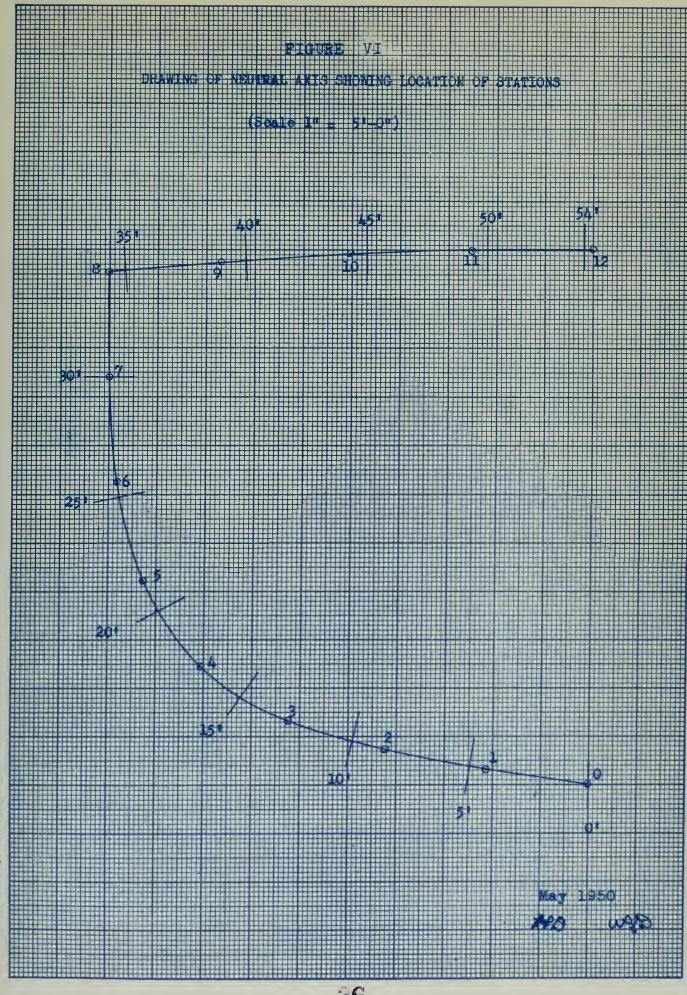
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-1	959.782	4.661
2	959.782	4.661.
3	896.714	5.026
Łį.	775.415	4.625
5	511.364	4.032
6	484.003	3.905
7	423.970	4.590
8	412.114	4.516
9	394.694	4.410
10	377.662	4.303
11	350.306	4.128
12	329.239	3. 988
13	396.971	1.678
14	377.692	1.620
15	352.859	1.543
1.6	277.395	1.224
17-25	253.118	1.914













APPATIDIN B

Description of the Model Design, Ennufacture, and Testing Procedure for Obtaining Influence Lines of the Redundants

Theoretical Principle

The determination of influence lines for redundants by experimental means is based on the Miller-Breslau principle. This principle states:

The ordinates of the influence line for any stress element (such as axial stress, shear, or moment) of any structure are proportional to those of the deflection curve which is obtained by removing the restraint corresponding to that element from the structure and introducing in its place a deformation into the primary structure which remains.

Prof. G. J. Begs has developed a method and the necessary equipment for application of the Müller-Breslau principle to the analysis of structures. The equipment consists of a model of the structure, a Begs deformeter gage, and a micrometer microscope. The Begs method is fully described in references (1) and (6). Its application to this investigation will be discussed under the testing procedure of the model.

The development of the application of this principle follows. Consider the axial thrust developed during application

^{1.} Wilbur, J. B. and C. H. Horris, Elementary Structural Analysis, ReGraw-Hill Book Co., New York, 1948, p. 450.

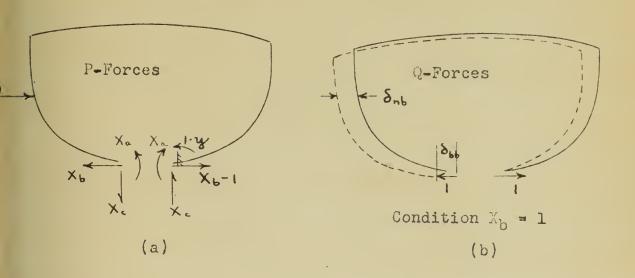






of a horizontal unit load at thoun in Figure VIIIs. Betti's Law states that the external virtual work done by a system of forces, P, during the distortion caused by a system of forces, is equal to the external virtual work done by the distortion caused by the P system.

Figure VIII



Applying Betti's Law to Figure VIII we can write:

$$\delta_{\rm b} = 0 = 1.8 \, \rm nb + 3.58 \, bb$$
 (1)

$$K_{b} = -\frac{\delta nb}{\delta bb}(1) \tag{2}$$

Applying the Beggs method to equation (2) $\delta_{\rm bb}$ is equal to the distortion introduced by one type of plugs and $\delta_{\rm nb}$ is the deflection measured at any point by the microscope.



In a similar manner expressions for \mathbb{X}_{θ} and \mathbb{X}_{c} can be developed so that:

$$X_{a} = -\frac{na}{aa} (1) \tag{3}$$

$$X_{e} = -\frac{DC}{CC} (1) \tag{4}$$

Design of Model

The model used with the Beggs deformater gage consisted of a planar celluloid representation of the characteristics of the original transverse frame. It was decided to make the model from a sheet of celluloid 1/16 in. thick and to the scale of 1/2 in. - 1 ft. 0 in. The characteristics of the prototype represented by the model were the shape of the neutral axis and the moment of inertia. These were obtained at 41 points spaced 16 in. apart along one-half the girth by reading the values from the curves represented by Figures IV and V in Appendix A. This large number of points was used to make the model closely approximate the actual variation in the moment of inertia. Similitude between the model and the prototype was attained by making the axial length k times that of the prototype and the moment of inertia of the model cross sections ∝ times those of the prototype. From this similitude, the ordinates to the influence lines for axial stress or shear on the model are equal to those on the prototype, but the ordinates of the influence line for any moment on the prototype are equal to 1/k times the corresponding ordinates on



the model. The scale of the model defines the proportionality fresor k=1/24. The proportionality constant, alpha (\propto), was assigned the value of 1/740,000. The selection of this constant determined the depth of the frame. This was limited to the $3/4^n$ maximum that the Beggs deformeter gage can accommodate. The development of the formula for the determination of the depth of the model follows:

$$\alpha = \frac{I_m}{I_p} = 1/740,000$$
 (5)

$$b = 1/16^{m}$$

$$I_m = \frac{1}{12} \text{ bh}^3 = \frac{h^3}{192} = \alpha I_p$$
 (6)

$$h = \sqrt[3]{192 I_p} = \sqrt[3]{\frac{192 I_p}{740,000}} = 0.06375 (I_p)^{1/3}$$
 (7)

The offsets, given in Table IV, for the curve of the neutral axis were determined by first drawing the molded line and then laying off the distances to the neutral axis.

Manufacture of Model

The model was manufactured by plotting the neutral axis on the sheet of celluloid. Half of the frame depth, as determined by equation (7), was laid off on each side of the neutral axis. The model was first sawed out and then filed to the proper depth. Table V gives a comparison of the actual depth of the model and the theoretical depth as determined by equation (7). Next the model was cut at the keel position and



Table 1V recording to get of Inertia for Januicht on Leatral wis

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3	13.00	464	12.50	2.67
l _v	17.40	400	16.12	4.90
5	21.3	358	11.54	0.42
6	26.20	344	19.66	12.54
7	30.5 0	372	20,01	16.00
S	35.00	263	20.05	21.11
9	4,0.13	253	15.40	21.53
10	45.27	253	10.04	21.04
11	50.04	253	5.02	21.99
12	55.25	253	0	20.05

Seutral Exit Girth-

4 at base to dit. on 0 = 31,1-3 3/6" = 34.261; 4 at dech to dk. ed e = 20:-1 1/2" = 20.125;

Station Secing on Beutral Mis 0-6 - 5 - 4.2051 8-12 - 8 = 3.0311

Origin ¢ at Base Line



Table V Model Jepth

Jution	I _p	h in.	Port Actual Depth in.	Stbd. Actual Depth in.
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Hot accurate -- due to same, a micrometer cannot be used satisf ctorily.



the ends rigidly clamped in the Beggs deformeter gage. The Beggs deformeter gage consists of two halves held together by springs. The right half of the gage was securely screwed to the table. With the deformeter gage are sets of plugs, which are inserted in the gage to make the two gage halves move relative to each other in rotation, horizontally or vertically. The plug sizes are such that one set causes relative rotation of 0.0104 radians, another set causes 0.0509° of relative horizontal displacement and the third set causes 0.0509° of relative vertical displacement of the ends. These distortions correspond to moment, thrust and shear, respectively.

The celluloid frame was supported at intervals by steel ball bearings resting on steel retainers. Weights were placed over the supports to make the frame stay flat. It was found that the weights produced frictional forces of sufficient magnitude to cause erratic results. To eliminate this, the weights were removed during the taking of data, and due care was used to be sure the frame remained flat.

Ordinates for the influence lines are to be determined for each of the 12 points along a half girth that were selected for use in the calculation of the influence lines. At these points, which were located on the model, microscope targets were glued.

A micrometer microscope was used to measure the deflections



which occurred at a point when each deformation was introduced by changing the plugs. Since the model was symmetrical,
the redundants on the starboard side of the cut are either
equal to those on the port side or differ from them by a
statically determinate factor. This factor is equal to the
support reaction corresponding to the redundant being considered.
As a check on the measured deflections the starboard deflections were also measured. At a number of places, due probably
to frictional effects, the redundants found from deflections
of the port side were not consistent at all points. At these
points the values used for the influence lines were the averages
of the port and starboard deflections. The starboard readings
used appear with the original data in Table XIX.

The deflections measured with the microscope are in microscope units. To apply the Müller-Breslau principle they must be in inches. The movement of a target on the plunger of an Ames dial indicator was measured in microscope units. This movement was compared with the movement registered in inches by the Ames dial. The calibration data are shown in Table AVIII, Appendix 3. A calibration constant of .000186 inches per microscope unit was used throughout the experiment.

Evaluation of Influence Line Ordinates

Equations (2)-(4) and the similitude proportionality factor k form the basis for the calculation of the ordinates



of the influence lines.

In evaluating these expressions the average deflections for S_{na} , S_{nb} , and S_{nc} given in Table XIX were used. The results are shown in Tables I and II.



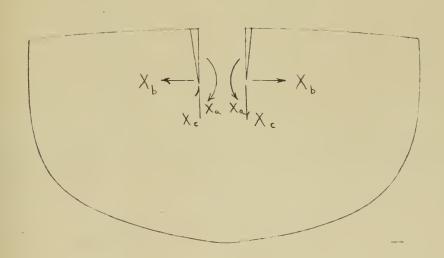
APPINDIA C

Calculation of Influence Lines by the Elastic Center Method

The elastic center method consists of a special application of the law of virtual work, in which location of the redundants at the elastic center simplifies the solution of the equations. The method and the equations are derived in reference (4).

The effects of axial stress and shear are a small order of magnitude and were neglected. The positive direction of the redundants will be as shown in Figure TK. Applying the

Figure IX



law of virtual work to this frame we can write the equations:



(1)
$$\delta_a = 0 = \delta_{a0} + X_a \delta_{aa} + X_b \delta_{ab} + X_c \delta_{ac}$$
 (8)

(1)
$$\delta_b = 0 = \delta_{bo} + \chi_a \delta_{ba} + \chi_b \delta_{bb} + \chi_c \delta_{bc}$$
 (9)

(1)
$$\delta_c = 0 = \delta_{co} + X_a \delta_{ca} + X_b \delta_{cb} + X_c \delta_{cc}$$
 (10)

In the above equations & refers to a deflection and X to a redundant force. The first subscript names the point whose deflection is under consideration at the moment and the direction of that deflection, while the second names the cause of the distortion. The subscript, o, indicates known external loadings.

By locating the redundants at the elastic center δ_{ab} * $\delta_{ba} = \delta_{bc} = \delta_{cb} = \delta_{ac} = \delta_{ca} = 0$. Thus it is found that equations (8)-(10) simplify to

$$X_{a} = -\frac{\delta_{a0}}{\delta_{aa}} \tag{11}$$

$$X_b = -\frac{\delta_{bo}}{\delta_{bb}} \tag{12}$$

$$\underline{\mathbb{Y}}_{\mathbf{C}} = -\frac{\delta_{\mathbf{C}\mathbf{C}}}{\delta_{\mathbf{C}\mathbf{C}}} \tag{13}$$

The location of the elastic center was first determined by equation (14).

$$\bar{y} = \frac{\int y \, \bar{1} o \, ds}{\partial \bar{1}_0 \Lambda_e} \tag{14}$$

y = distance from assumed axis to the elastic center

A - elastic Weight

Io was arbitrarily assumed = 960 in4



Integration of equation (14) is shown in Table VI. Due to the symmetry of the frame, integration was carried halfway around and doubled. The elastic weight is equal to δ_{aa} and is evaluated by equation (15)

$$S_{aa} = \int M_a^2 \frac{ds}{EI} = \int 1^2 \frac{ds}{EI} = A_0$$

$$II_0 S_{aa} = EI_0 A_0 = \frac{2 \times 4.285}{3} \times 2 \times 51.8612 = 296.3003$$

$$\bar{y} = \frac{\frac{2 \times 8}{3} \times 830.0717}{\frac{2 \times 5}{3} \times 51.8612} = 16.0056 \text{ ft.}$$

The origin was assumed at the molded base line on the centerline of the ship. The elastic center is located at y = 16.0056 ft. and, due to symmetry about the y axis, at x = 0. Let yo be the vertical distance from a point to the elastic center. δ bb was determined from equation (16). The integration of this equation is shown in Table I.

$$EI_0 \delta_{bb} = \int H_b^2 \frac{I_0}{I} ds = \int y_0^2 \frac{I_0}{I} ds$$
 (16)
= 3121.1653 x $\frac{2 \times 4.285}{3}$ x 2 = 17,832.2576

Scc was determined from equation (17). The integration of this equation is shown in Table VI.

ELoSec =
$$\int_{-\infty}^{\infty} \frac{1}{1} ds = \int_{-\infty}^{\infty} \frac{1}{1} ds$$
 (17)
= $10748.5039 \times \frac{4.285 \times 2}{3} \times 2 = 61409.7811$



Integration to Jetermane Saa, Sub, and See

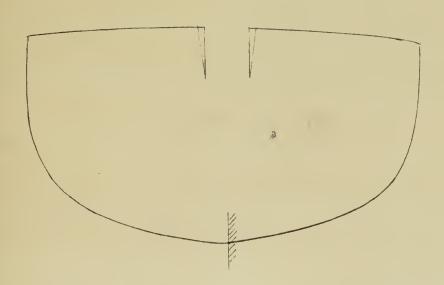
10/10 - 10 C	9	38,9552	1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1	646.5525	505,9302	2043.2.33	1000 OF 00	2000,3450	3330000	667.3/03	222. 770	5040.547	224,5230	10:48.5030
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L. C.	3006	8	1. 1925	4.1380	2.3472	3000	2002			7	\$,9095	245年中	6,9095	4 N 100 C
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The second second	055%*	2.0000	1,1925	0.690	2.3472	2.070	1982	2,5006	3,6502	3,6502	3.7945	3,7545	3.7945	3.79%
	3	00:	÷ ⊕.	3000	5.00	3	다. (1) (1)	10 7	64	27.49	27.01	22.22	2000	52.73
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	12	(<u>j</u>	٠.	m		4.7	4,2	- Marie - Mari	10	N.S.	ij'n	ş Şung	- E	<u>63</u>

w pin son's initial liters



In the stress analysis of this frame influence lines for the redundants caused by (1) a unit vertical load and (2) a Lit horizontal load were determined. A stable and statically determinate structure that remains after the removal of the redundant forces is called a primary structure. Figure I shows the primary structure assumed.

Figure X



Ho is the bending moment in the primary structure caused by a unit load applied at a given point. For the primary structure

$$S_{20} = \int I_2^2 N_0 \frac{10}{1} ds = \int I_0^2 \frac{10}{1} ds \qquad (13)$$

$$\delta_{DO} = \int W_D N_D \frac{1}{I} ds = \int N_D y_D \frac{1}{I} ds \qquad (19)$$

$$S_{co} = \int M_c M_b \frac{1}{I} dz = \int M_b X \frac{1}{I} dz \qquad (20)$$

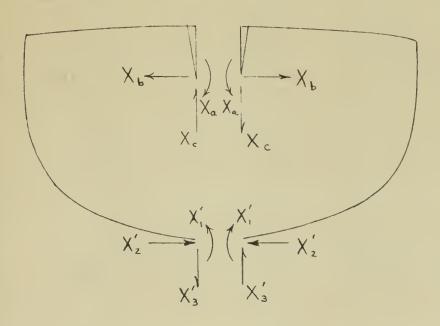


The integrations of S_{ao} , S_{bo} , and S_{co} are shown in Table VII for a unit horicontail load. The redundants are evaluated by equations (11)(13). The numerical evaluation of these is shown in Table
IX for a unit vertical load and in Table X for a unit horicontail load.

The values obtained for the redundants located at the elastic center are different from those obtained experimentally because of the difference in the location. Figure XI shows the two locations and the positive sense of the redundants.

Equations (21)-(23) give the relationship between the redundants

Figure XI



at the two locations when a vertical load is applied on the port side of the frame.



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11000000	+ 127.2475 + 127.2475 + 180.1631 + 514.7230	at Point 4p	+ 356.6275 + 356.6331 + 128.6761 + 124.0693 + 750.1050 + 750.1050	at Point op	+ 122,7256 + 462,7727 + 12, 5909 + 383,6497 + 1269,6413 +3664,0752
Sport	3,3875 6,400 0 11,6678 - 33,9023	Load	23.7600	Lond	7.8542 30.8400 113.3323 29.5261 6.0068 6.0068 7274.1554
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	0 0 1.6939 - 4.8389 +	Load at	16.5200 + 4.7939 + 0.000 + 0.0	Load at	20067 + 21.9966 + 24.9935 + 5.6802 + 5.6802 + 7.85.670 + 7.85.6802 + 7.85.670 + 7.85.670 + 7.85.670 + 7.85.670 + 7.85.670 + 7.85.6802 + 7.
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at Point Sp	No Loydo	+ 125 169 + 125 169 + 126 169	+3956 +3956	+ 62.6737 +174.0650 -153.6613 -153.6613 + 262.4614 +282.4614 +142.263 +406.4565
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at Point Sp	Mologo	131,7771 614,9295 -331,1306 -988,5739 -408,0684 -400,4063 + 26,3466	t Poi	-136 3340 -636 8377 -343 4447 -1027 7095 -426 4662 -518 6172 -518 6172 -16 9271 -16 9271 -16 3352 -3105 4203 -3105 4203
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Elosbo Ho <u>lo</u> yds	0	+ 75.6097	+ 514.7230	+1124.7676	+2228,5026	+3140.3973	+3684.0752	+3865,2090	+3956.8997	+1894.2779	+ 406.4565	- 589.3586	- 770.7398	110850 = 17832.2576
रह १-व	0	+ .0163	4.1144	+ .2536	+ .5234	+ .7585	+ .9253	+ .5868	+1.0184	2308	-2.1051	-4.0761	-6.4783	3003
Llosao 1010de	0	- 4.8389	- 33.9023	- 75.1523	- 155.0890	- 224.07540	- 274.1554	- 292,3830	- 301.7611	+ 68,3817	+ 623,7323	+1207.7375	+1919.5097	Elobaa = 296.3003
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Calculation of Adundants at Mastic Jenter due to Hori sontal Load

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LI Colo	0	- 11,0562	-100,1216	-280.7069	-960.6321	-2287.0247	-4294.3389	-6474.6534	-\$605,2953	-8785.1011	-8871.1504	-8900.5055	-\$903.0727	1360h = 1783 2576
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CO CO CO CO CO CO CO CO CO CO CO CO CO C	0	<i>r</i> -1	R	~	オ	N	ග	2	10	C	O ri	hang bang	"Sung Cong	



$$x_1 = x_2 - y_0 x_1 - x \cdot 1 \tag{21}$$

$$X^{\bullet}_{2} = X_{b} \tag{22}$$

$$1.13 = 1. -1$$
 (23)

Iquations (24)-(26) give the relationship between the redundants at the two locations when a horizontal load is applied on the port side of the frame.

$$X_1 = X_2 - \lambda^0 X^0 + \lambda_0 T$$
 (54)

$$X^{*}_{2} = X_{b} - 1 \tag{25}$$

$$X^{1}_{3} = X_{c} \tag{26}$$

The evaluation of equations (21) and (23)-(25) is shown in Table XI for a unit vertical load and in Table XII for a unit horisontal load.



Transfer of Redundants to Relocate at Station O Due to Unit Vertical Load

(x, x, 2, 1)	-1,0000	3 -1.001673	9-1.005149	-1.0170	-1.0202	-1.0400	-1.0443	-1.0467	9840	- :034	6969. ~	
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(Xayokb-x)	4.1574	- 7.9246	-11,2609	-13.6439	-15.0147	~15.5065	-15.6364	-15.5643	-13.9709	-11.7390	- 9.6125	- 7,1536
ĸ	4.24	3.40	12.50	16.12	18,54	19.66	20.01	20.05	15.40	10.01	5.03	0
yozb za~yozb	9280. +	+ ,5054	+1.2391	+2.4761	+3.5253	+4-1535	+4,3736	*4.4857	+1.4291	-1.74.90	-4.5925	-7.1536
yo.k	0663	. 4510	~ .9855	-1.9527	3007.8	-3.2282	~3.3868	-3.4673	-1.6599	3561	+ .5164	+ ,6753
x p	.0163	+ •1144	. 2536	4625	.7565	. 9253	8996.	+1.0164	. 2300	~2.1051	-4.0761	622709
Stat.	0-1	CA CA	m	4 47	r v	9	+ 1.	20	O ₁	0.0	r-d	8 ~-i



Trunctor of Redundants to Relocate at station O Due to Unit Horizontal Load

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(Xa-yoXb+y)	e states parametral de la companya del companya del companya de la	.62 + .6079	1.48 + 1.370	+ 2,3605	+ 3.0286	+ 5.8443	+ 7.5911	+ 9.1028	+10,6638	+10.6139	+10.9416	+11,0067	+11.0361
>		.62	1.43	2.67	06.4	0 th	12.54	16.30	7	21.53	23,84	21,99	22,05
Xa~yoxb		012077	110031	- 300472	- 1.071436	- 2.575676	- 4.948941	- 7.607213	-10.446216	-10.716101	~10.898367	-10.983326	-11.013943
od Por		+ .009689	+ .087738	+ .245978	+ .841751	+2.004014	+3.762941	+5.673452	+7.540430	+7.697983	+7.773392	+7.759456	+7.501362
\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\		002338	. 022283	767690 -	- 229687	571564	-1.186000	-1.933761	-2.905786	-3.010118	-3.124975	-3.133570	-3.212581
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							100	- 4 "					



APPENDIN D

Calculation of Influence Lines for the Redundants by the Hovgaard Nethod

The cheral nathematical treatment and applications of the formulae are described by Dr. Milliam Hovgmand in reference (5).

Briefly, the procedure followed was to apply a unit vertical load at one station and solve for the redundants.

This was repeated for every station; then the whole procedure was repeated for a unit horizontal load. The results were plotted as a family of influence lines.

The following assumptions were made:

- (1) The neutral axis of the ship frame forms a continuous closed curve, interrupted by a point of sharp curvature at the deck edge.
- (2) The intersection of the neutral axis with the centerline just above the keel was used as the origin of coordinate axes, and was the place at which the bending moment, thrust and shear were found.
- (3) Only the deformation caused by bending was considered; deformations caused by axial and shear forces were neglected.

The equations fundamental to the Hovgaard method are:

$$\int_0^\infty \frac{31}{1} ds = 0 \tag{27}$$



$$\int_0^\infty y \frac{y}{1} ds = 0 \tag{28}$$

$$\int_0^\infty x \, \frac{M}{I} \, ds = 0 \tag{29}$$

where:

W = bending moment at a point due to all forces

x = Lorizontal coordinate of a point

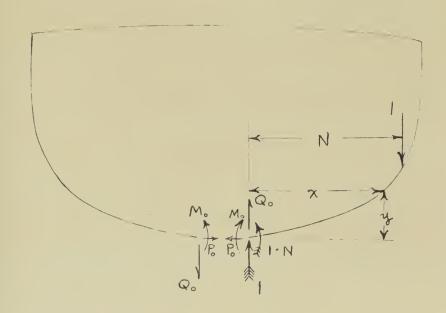
y - vertical coordinate of a point

I = noment of imertia

Inch units ere used for moment of inertia; kip and feet units were used for other terms.

The value of M depends on the loading system and the nature of the redundants. In Figure XII the redundants are

Figure XII



shown in their positive sense. A unit vertical load was



station 0 in order to maintain equilibrium. The support reactions vanish when actual use is made of the influence lines. The moment at any station (A) is

$$N = N_0 + P_0 y + Q_0 x + 1 \cdot x - 1 \cdot N$$

$$= N_0 + P_0 y + Q_0 x + N + x$$
 (30)

Integration was done halfway around the frame and advantage taken of symmetry. Simpson's rule was used for integration with eight stations selected between the heel and the deck edge, and four more stations selected between the deck edge and the center of the deck. The spacing of stations 0 to 8 was 4.285 feet and of stations 6 to 12 was 5.031 feet. All terms were divided through by 4.205, yielding "station factors" of 1 and 1.174, which were easier to tabulate.

Use was made of Professor G. C. Hanning's method of organizing the work in the following equations.

Substituting W in equation (27)

$$\int \frac{ds}{1} ds = \int \frac{ds}{1} \left(M_0 + P_0 y + Q_0 x \neq N + x \right) = 0$$
 (31)

Integrating term by term with Simpson's rule we have

$$\int \frac{1}{1} ds = H_0 \frac{23}{3} \left(\frac{1}{2I_0} + \frac{2}{I_1} + \frac{1}{I_2} + \frac{2}{I_3} + \dots + \frac{1}{2I_{12}} \right) = \frac{23}{3} \propto H_0$$
(32)
$$\int \frac{P_0 V_{cls}}{1} ds = P_0 \frac{23}{3} \left(\frac{V_0}{2I_0} + \frac{2V_1}{I_1} + \frac{V_2}{I_2} + \frac{2V_3}{I_3} + \dots + \frac{V_{12}}{2I_{12}} \right) = \frac{23}{3} \beta P_0$$
(33)



$$\int \frac{1}{1} ds = \sqrt{3} \left(\frac{x_0}{2I_0} + \frac{2x_1}{I_1} + \frac{x_2}{I_2} + \frac{2x_3}{I_3} + \dots + \frac{x_{12}}{2I_{12}} \right) = \frac{20}{3} \chi_{20}$$
 (34)

$$\int \frac{(x-1)}{1} ds = \frac{25}{3} \left(\frac{x_0-11}{2L_0} + \frac{2(x_1-11)}{L_1} + \frac{x_0-11}{L_2} + \frac{2(x_1-11)}{L_3} + \dots + \frac{x_{12}-11}{2L_{12}} \right) = \frac{25}{3} \varepsilon (35)$$

Substitute (32) (33) (34) and (35) in equation (31), divide through by $\frac{23}{3}$ and the result is

$$\propto 10 + 3P_0 + 80_0 + E = 0$$
 (36)

si ilarly, from equations (28) and (29), one may derive:

$$\propto_{2}\mathbb{N}_{0} + \beta_{2}\mathbb{P}_{0} + \gamma_{2}\mathbb{Q}_{0} + \varepsilon_{2} = 0$$
 (38)

The values of ε , ε_1 and ε_2 depend on the external loading system.

The values of α , β and δ are constant. In Table IIII are found the values of $\frac{\alpha}{2}$, $\frac{\beta}{2}$, and $\frac{\delta}{2}$. Doubling ives:

The values of E, E, and E, were found, for the vertical load, by the integrations shown in Table MIV.

The simultaneous equations (36), (37) and (38) were solved in Table. NVI and XVII.



Hable Hill How Goard Stund Calculation of Coefficients of For Por and to

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(13)	20 20 20 20 20 20 20 20 20 20 20 20 20 2		00000 00000 00000		99999999999999999999999999999999999999
(2)x(2)x)	0000		072345 042270 0	v)	126112 105781 325405 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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(14) x-1;		25555550 25555550 25555550 25555555 2555555 2555555 2555555 255555 255555 25555 25555 25555 25555 25555 25555 25555 25555 25555 255 2		111++++++ 07446000000
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()1 ×		000454m		255555500 25555555500 255555555500
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stat.		○ 0		046476764010



(14) ϵ_{-1} (7)×(14) (6)×(14) (9)×(14)	Load at Station 120	+ 6.24 + 0.05019 + 0.05470 + 0.37393 + 5.45 + 0.05019 + 0.05470 + 0.37393 +12.50 + 0.53075 + 14.3850 + 673438 +16.12 + 0.53075 + 14.3850 + 673438 +10.54 + 10.3564 + 872010 + 920077 +20.01 + 10.3564 + 872010 + 920077 +20.01 + 10.7574 + 80.7243 + 2.152556 +20.05 + 0.62867 + 74.9322 + 1.661433 +15.40 + 1.42927 + 0.77226 + 2.201076 +10.04 + 0.46586 + 0.17434 + 467723 + 5.02 + 0.6591 + 0.24527 + 2.33087 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
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		00000000000000000000000000000000000000
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Stat. (13)		いているなりないない。



liov aard lethod Calculation of E , E, and Ez due to Unit Horizontal Load

(7)x(14) (8)x(14) (9)x(14) Load at Station 28	6 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	t Station ha	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	at Station 6s	4 + 015377 + 105122 4 + 020295 + 116296 6 + 113584 + 531746 2 + 091344 + 300504 4 + 193780 + 126681 0 0 0 1 + 434380 + 150352
(41)×(14)	+.000616 +.001789 0 +.002405	Load at	+ 002040 + 0005002 + 0005011 + 0005011 + 024794	Load a	+.005220 +.024794 +.013714 +.012540 +.023014 0
(14) 7-11	1.43		4.28		11.052 11.052 10.052 10.052
3:1	1200		20000		यंत्रेयंत्रेयंत्रेयं विवेद्यात्रेयंत्रेयं
E, (8)x(14) (97x(14) ii t station le	000	S)	+.012079 +.012513 0 +.030592	5.23	+,068788 +,072974 +,3057814 +,130452 0
8 (31%) Section 16	000	Stetion 3	+.0022645 +.002184 0 0 +.004829	tation	-010062 +012735 +056171 +042005 +131053
(71×(14)	+.000258 0 +.000258	Doad at	+.001112 +.0011764 +.001476 0	Load at.	+.003505 +.016224 +.013763 +.013763 003569 0
35	•00		2.67		######################################
(5)	, , , ,		000000 000000		00000000000000000000000000000000000000
t gat	0 1 2		15 15 15 15 15 15 15 15 15 15 15 15 15 1		6-12 6-12



(41) (9) (41) (14)	Ltation de	+ 026432 + 160701 + 036021 + 206409 + 212208 + 993455 + 193607 + 637558 + 56661 + 937558 + 312411 + 469793 + 349266 + 465644	ct.clon 10a	+ C2/374 + 167139 + 037361 + 114065 + 220608 +1.032784 + 202535 + 566301 + 631197 +1.399629 + 339022 + 5631514 + 651197 +1.309629 + 063691 + 04,4307 0 0 0
(41) (41) \$(2)	Load at	+ 0005768 + 042619 + 024341 + 079476 + 079476 + 079856 + 024913 + 024913 + 023171	Load at	+ 009092 + 044138 + 044138 + 042623 + 041334 + 074964 + 074964 + 074964 + 074964 + 074964 + 074964 + 074964 - 0779964 - 07799664 - 0779664 - 0779664 -
(174) X=11		1250 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5		00000000000000000000000000000000000000

(4/2/2/2)		- 142691 - 142691 - 161090 - 1		+,151,405 +,210826 +,016083 +,654108 +,557724 +,508625 +,508625 +,034804
(4) (4) (5) (4) (13) (13) (13)	tertion 7a	- 023112 + 162608 + 394145 + 155294	Tration 9s	+ 0365974 + 036792 + 217041 + 515616 + 527721 + 327721 + 127199 + 036644
(J.)	Loa: et	+ 00.0000 + 00.00000 + 00.000000 + 00.000000 + 00.0000000 + 00.00000000 + 00.00000000000000 + 00.0000000000000000000000000000000000	ad at	+ 0000963 + 040577 + 040577 + 073232 + 026134 + 026134 + 026134 + 026134 + 026134 + 026134 + 026134
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Hovgaard lethod--Vertical Unit Load solution of Simultaneous Lautions

Load a	t Coef. of	Coef. of	0513528	No	1-17	1.4%
1	.108020 06687 .021333	1.688090 1.688090 0	+.001765 001765	+ .0327	- 4.2h	- 4.1573
2	4.	12	+.012349 +.000281 +.012008	+ .5657	- (.48	- 7.9143
3	£3		+.027370 +.000926 +.026444	+1.2396	-12.50	-11.2604
l _e	23	ŶŶ	+.056497 +.003646 +.052851	+2.4774	-16.12	-13.6426
5	99	TF .	+.061873 +.006950 +.074923	+3.5121	-18.54	-15.0279
6	\$₹	3	÷.099875 +.011185 +.088690	+4.1574	-19.66	-15.5026
7	ęş	· **	+.106517 +.013163 +.093354	+4.3760	-20.01	-15.6340
đ	€2	73	+.109933 +.014189 +.095744	+4.4881	-20.05	-15.5619
9	D	1 17	024978			-13.9875
10	25	13	227422 189282 038140			-11.0278
11	\$7	ŶŶ	440317 341068 099249			- 9.6724
12	Ħ	π	699803 545464	-7.2348		- 7.2348
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0)	0	0	0	0	0	0	1.0000
rel	7,068090	055937	4. 301765	0043	22,355912	0	0	1.0000
64	#1-0 4	061106	4,012349	- 0289	⊕ -to gun	+,037393	+ 0017	1,0017
7	photo to to	-,133900	*,027370	0631	gino gras	4.115115	+.0051	1.0051
and the same of th	Pas yre	267607	+,056497	-,1251	ghapa Bross	+,380133	+.0170	1,0170
201	Orange Lijeres	**379374	4,081273	1762	gion ban	+.652464	1620.+	1,0291
S	desga Evir	£306474500	4.099875	. 2009	Spars Spars	+,594523	\$ 00°00	1,0400
2	genn gen	472700	+.106517	~,21.69	Uno San	+.990162	+,0442	1.04,42
ಎ	Qury Grave	-,404,301	+,109933	. 222	Q _q (Pare Base)	+1.044729	+.01,67	1.0467
0	direct Spree	152574	024972	2001.	\$ 10 10**-	-1.150805	0514	9546.
10	Qiron que ti	+.193122	- 227422	. 0203	Zpop apris	-1, 402322	-1966	\$6034
r-4 r-1	#	+,502549	446317	÷.0369	€1-0- €1-14	-7.681,43	3431	6957.
N ed	100 er \$1-10	4.7.1493	£02069 °-	****	po-s	-11,194456	~,5000	.5000



Table XVII Hov and Method-Horisontal Unit Load Solution of Siguitaneous Squations

Load	at Coof. of	Coef. of	0513528	i No	1•V	V+10
1		1.683090 1.683690 0	000258 0 000258	0121	.62	÷ .6079
2	· If	9 d 1 d	002405 000057 002348	1101	1.43	+ 1.3699
3	12	¥?	006352 000248 006604	3096	2.67	+ 2.3604
4,	13	13	024794 001924 022870	- 1.0721	4.90	+ 3.8280
5	13	17	060707 006730 053977	- 2.5302	0.42	+ 5.0898
6	St	\$\$	127924 022306 105618	- 4.9509	12.54	+ 7.5391
7	18	17	208776 046387 162389	- 7.6121	16.00	+ 9.1879
Ė	17	12	313746 090740 223000	-10.4536	21.11	+10.6564
9	11	15	325712	-10.7237		
10	i7	*&	337421 104704	-10.9088		
11	77	11	3437\$1 109239	-10.9943		
			346883 111682			
12	17	;;	235201	-11.0252	22.05	+11.0248



50.9	0	0	00003	0014	00057	#0000°	66.7	;! ;!	1914	-, 2001	- 2085	- 2129	
\$ 5 m	0	0	4857.00	030592	193847	5.6.5	1	-2.C.	-4.205017	-4.4.10571	-4.663625	-4.766606	965803.4-
Coef. of	22,328912	Street 6 =	E to their	₹779 €~*	glangs burn	fins See	from ty -	do- to-	P+v q.~	(from darm	=	f on	freq the
K 0	-1.0000	7666	\$74766	£489	1946	THE WAR	1355	~ .6366	5169	. 5067	. 5018	. 5001	- 500c
200		90000*	+.0056	+,0158	+.0539	+,1259	+.2410	+.3634	4.4032	+.4933	4. C. S.	5667*+	4.5000
Ψ		000258	002405	006852	024794	202090	-,127924	208776	313746	325712	337421	343781	346853
-10802016		+ .001306	÷ .011889	+ .033439	* .115803	+ .273313	+ .534798	+ .022259	+1,129195	+1,150371	+1,176366	+1.187607	+1.190944
Coef. of	e©-sever (B) ○ december de se de l'eve _t - della colde i de	1.663090	Story Lori	E Tridas Selection	Phon Bank		grape spread	Ent to the	⊕re grek	gives Jane	erson Gr	A-m	gran Surra
No d at	0	m	ત્ય	~	47	70	©	-	ಬ	6	207		73 (~1



In the forejoin only a vertical load has been considered. In considering a horizontal load equation (30) would be

$$M = H_0 + P_0 y + Q_0 x - 1 \cdot y + 1 \cdot H$$
 (39)

where it is the vertical distance from the origin to the point of application of the load. Equation (35) would be

$$\int \frac{(1-y)}{I} ds = \frac{20}{3} \left(\frac{11-y_0}{2I_0} + \frac{2(11-y_1)}{I_1} + \frac{(1-y_2)}{I_2} + \frac{2(11-y_3)}{I_3} + \dots + \frac{(1-y_{12})}{2I_{12}} \right) = \frac{2S}{3} \in (40)$$

The values of \mathcal{E}_1 , and \mathcal{E}_2 were found for the horizontal lower by the integrations shown in Table XV.

The moment, thrust, and shear obtained were the values nust to the right of the support reactions. They differ from the values just to the left by the amount of the support reactions. For comparison with the values found experimentally and by the clastic center method the values to the left were desired. The conversion was made by allebraic addition of support reactions as follows:

For vortical load,	moment	1-11
	thrust	no change
	shear	1
For horizontal load	, moment	1.V
	thrust	1
	shear	no change

The computations are done in Tables IVI and IVII.



APPENDIX E

Original Data

T.



Table XVIII

Read.	Cal Ames Dial Inche	Microso Reading	•	e Ames Dial Inches	Microscop Rending Divisions	e Diff.
23456	0 .015 .030 .045 .060	114.9 195.7 276.7 360.4 440.6 521.0	80.8 81.0 83.7 80.2 20.4 406.1	0 .020 .040 .060 .080 .100	03.7 169.1 279.5 387.4 494.0 601.2	105.4 110.4 107.9 106.6 107.2 537.5
Calibr	ation	Constant	0.0001847			0.0001861
1 2 3 4 5 6	0 .015 .030 .045 .060	77.4 158.1 238.9 321.8 402.6 483.9	\$0.7 \$0.8 \$2.9 \$0.8 \$1.3 406.5	0 .020 .040 .060 .000	77.3 185.7 294.2 402.8 509.8 615.9	108.4 108.5 108.6 107.0 106.1 538.6
Calibr	ation	Constant	0.0001845	gjauggar sjóknjaljá-filmák nadál mejkhnyáljála		0.0001860
1 2 3 4 5 6	0 .020 .040 .060 .080	176.6 284.3 393.5 502.1 609.8 714.5	1.07.7 1.09.2 1.08.6 1.07.7 1.64.7	0 .020 .040 .060 .080	69.3 176.7 234.4 392.7 499.8 605.8	107.1 107.7 108.3 107.1 106.0
Calibr	ation	Constant	0.000186			0.000186



Junet Rand, Diff.	25 H 405.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0 5.0		
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